

# Vectors (p. 119 - 125)

## I. Vectors In Multiple Dimensions

1. Vectors consist of the properties Magnitude and direction.

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2. How are vectors added together to find the resultant?

Placing them tip to tail, draw resultant, connect tail of first vector to tip of second vector.

3. If you move a vector so the length and direction are unchanged, the vector is unchanged.

Circle One :

True

False

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4. The resultant of a vector is drawn from the tip of the first vector to the tail of the second vector.

Circle One :

True

False

5. Write out the formula for the Pythagorean Theorem.

For angles with 90° →

$$R^2 = A^2 + B^2$$

Squaring a House, Deck, or Driveway

6. When is the Pythagorean Theorem used when adding vectors?

To determine the hypotenuse (R, resultant) a.k.a. →

7. Write out the formula for the Law Of Cosines.

For angles greater than 90° →

$$R^2 = A^2 + B^2 - 2AB \cos \theta$$

8. Write out the formula for the Law Of Sines.

$$\frac{R}{\sin \theta} = \frac{A}{\sin a} = \frac{B}{\sin b}$$

9. When is the Law Of Cosines or Law Of Sines used when adding vectors?

When vectors are added at angles other than 90°

## II. Components Of Vectors

1. What are good recommendations for placing a coordinate system when :

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	X-Axis	Y-Axis
Motion is on the surface :	<u>Point East</u>	<u>Point North</u>
Motion is in the air :	<u>Horizontal</u>	<u>Vertical</u>
Motion is on a hill :	<u>Direction of motion</u>	<u>Perpendicular to x-axis</u>

2. Define the term components.

Components - vectors parallel to the x-axis and another parallel to the y-axis  
 ( $A_x$  = parallel to x-axis) ( $A_y$  = parallel to y-axis)

3. Complete the following equation relating to components.

$$A = A_x + A_y$$

(Not the same as Pythagorean Theorem)

4. Define the term vector resolution.

Vector Resolution - process of breaking a vector into its components

5. The magnitude of an original vector is always larger than either component vector.

Circle One : True False

6. For the direction of angles, the angles are measured clockwise.

counterclockwise

Circle One : True False

7. Complete the missing parts of the equations.

(Used only for right triangles!)

$$\cos \theta = \frac{\text{adjacent side}}{\text{hypotenuse}} = \frac{A_x}{A} = A_x = A \cos \theta$$

$$\sin \theta = \frac{\text{opposite side}}{\text{hypotenuse}} = \frac{A_y}{A} = A_y = A \sin \theta$$

$$\tan \theta = \frac{\text{opposite side}}{\text{adjacent side}} = A \tan \theta$$

8. When are  $A \cos \theta$  and  $A \sin \theta$  used when calculating vectors.

To determine missing vector sides of a triangle.

CAH-SOH-TOA

### III. Algebraic Addition Of Vectors

1. Assuming three vectors (A, B, C) combine to form a particular resultant (R), what equations are used to determine the following?

$$R_x = A_x + B_x + C_x = \sum R_x$$

(Vertical Line - parallel to y-axis)

$$R_y = A_y + B_y + C_y = \sum R_y$$

(Horizontal Line - parallel to x-axis)

$$R^2 = R_x^2 + R_y^2 = R = \sqrt{R_x^2 + R_y^2}$$

2. Identify the two other equations used to determine angles with right triangles and when they are used.

On Calculator

When Used

$$\theta = \tan^{-1} \left( \frac{R_y}{R_x} \right)$$

- when opposite and adjacent sides known.

$$\theta = \cos^{-1} \left( \frac{R_x}{R} \right)$$

- when adjacent and hypotenuse sides known.

$$\theta = \sin^{-1} \left( \frac{R_y}{R} \right)$$

- when opposite and hypotenuse sides known.

1. Push  $\tan^{-1}(\text{value})$   
2. Divide by 10  
(If set for radians!)

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